

# Letters to Nature

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## Optimal traffic organization in ants under crowded conditions

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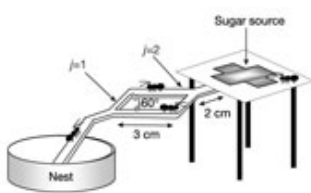
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**Efficient transportation, a hot topic in nonlinear science<sup>1</sup>, is essential for modern societies and the survival of biological species. Biological evolution has generated a rich variety of successful solutions<sup>2</sup>, which have inspired engineers to design optimized artificial systems<sup>3,4</sup>. Foraging ants, for example, form attractive trails that support the exploitation of initially unknown food sources in almost the minimum possible time<sup>5,6</sup>. However, can this strategy cope with bottleneck situations, when interactions cause delays that reduce the overall flow? Here, we present an experimental study of ants confronted with two alternative routes. We find that pheromone-based attraction generates one trail at low densities, whereas at a high level of crowding, another trail is established before traffic volume is affected, which guarantees that an optimal rate of food return is maintained. This bifurcation phenomenon is explained by a nonlinear modelling approach. Surprisingly, the underlying mechanism is based on inhibitory interactions. It points to capacity reserves, a limitation of the density-induced speed reduction, and a sufficient pheromone concentration for reliable trail perception. The balancing mechanism between cohesive and dispersive forces appears to be generic in natural, urban and transportation systems.**

Animals living in groups<sup>7,8</sup> often display collective movement along well-defined lanes or trails<sup>9,10,11,12,13</sup>. This behaviour emerges through self-organization resulting from the action of individuals on the environment<sup>14,15,16</sup>. In ants<sup>17,18</sup>, for example, mass recruitment allows a colony to make adaptive choices based solely on information collected at the local level by individual workers. When a scout ant discovers a food source, it lays an odour trail on its way back to the nest. Recruited ants use the trail to find the food source and reinforce it in turn on their way back to the nest. Without significant crowding, mass recruitment generally leads to the use of only one trail<sup>19</sup>, because small initial differences in pheromone concentration between the trails are amplified as greater numbers of ants choose the trail that was initially slightly stronger, and hence reinforce it. This, together with travel time, ant numbers and ant individual behaviours, also

explains why ants use the shortest among several paths leading to the same food source<sup>19, 20</sup>.

Here, we investigate the regulation of traffic flow during mass recruitment in the black garden ant *Lasius niger*. Ants were forced to move on a diamond-shaped bridge that formed two branches between their nest and a food source (**Fig. 1**). We studied to what extent the traffic on the bridge remains asymmetrical (and therefore limited by the capacity of one branch) when an increased level of crowding is induced by using branches of reduced width ( $w$  [equals] 10.0, 6.0, 3.0 and 1.5 [thinsp] mm). The temporal evolution of the flow of ants on the bridge shown in **Fig. 2** is typical of a trail recruitment process<sup>21</sup>. Surprisingly, the recruitment dynamics was not influenced by the branch width  $w$  and the traffic volumes were the same (analysis of variance, ANOVA,  $F_{3,44}$  [equals] 0.500,  $P$  [equals] 0.690). However, for  $w$  [equals] 10 [thinsp] mm, the majority of ants used the same branch (**Fig. 3a**), whereas for  $w$  [le] 6 [thinsp] mm most experiments led to symmetrical traffic ( $|\chi|_2$  [equals] 1.686, d.f. [equals] 2,  $P$  [equals] 0.430). This suggests that there is a transition from asymmetrical to symmetrical traffic between 10.0 and 6.0 [thinsp] mm ( $|\chi|_2$  [equals] 12.667, d.f. [equals] 3,  $P$  [equals] 0.005).

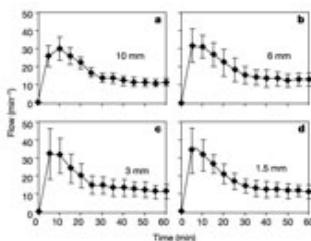


**Figure 1: Experimental set-up.**

Five queenless colonies of *L. niger* (Hymenoptera, Formicidae), each containing 500 workers, were used. During an experiment, ants had access from the nest to a source of food (2 [thinsp] ml of 1 [thinsp] M sucrose solution) placed at the end of a diamond-shaped bridge. The solution was spread over a large surface so that all ants arriving at the end of the bridge could have access to the food.  $j$  [equals] 1 and  $j$  [equals] 2 indicate the choice points for branch selection. The whole set-up was surrounded by white curtains to prevent any bias in branch choice caused by the use of visual cues. The colonies were starved for four days before each experiment. The traffic on the two-branch bridge was recorded by a video camera for one hour. Nestbound and outbound ants were then counted and aggregated over 1-min intervals. Counting began as soon as the first ant climbed the bridge. Four different bridge widths ( $w$ ) were used. This set-up mimics many natural situations in which the geometry of the trails is influenced by physical constraints of the environment, such as the diameter of underground galleries or of the branches in the vegetation along which the ants are moving.

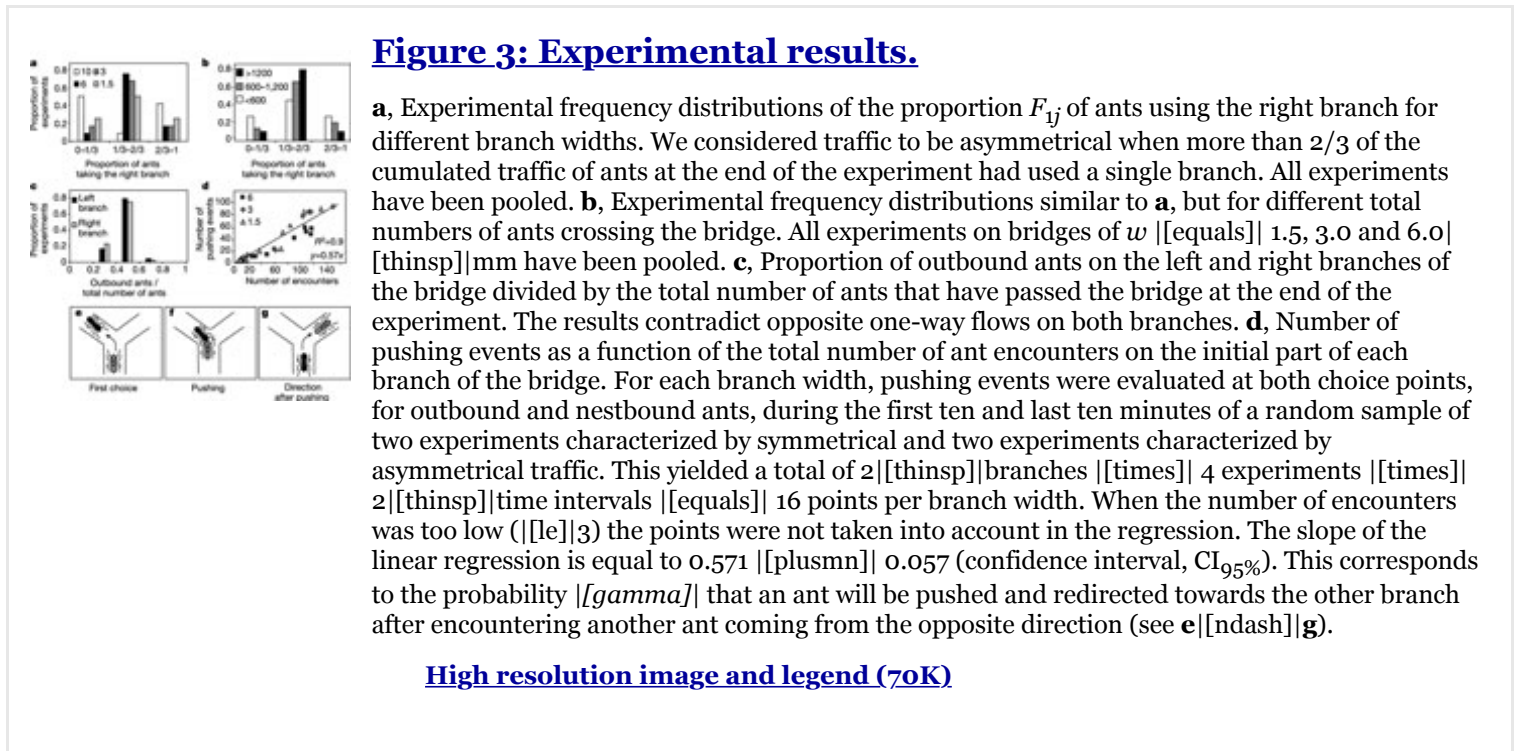
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**Figure 2: Average number of ants per minute crossing the two branches of the bridge within intervals of five minutes.**



The observed traffic volumes  $z[\mathit{phis}](t)$  and flow dynamics agreed for the four different branch widths, that is, the bottleneck for smaller branches was compensated for by use of both branches. **a**,  $w$  [equals] 10 [thinsp] mm; **b**,  $w$  [equals] 6 [thinsp] mm; **c**,  $w$  [equals] 3 [thinsp] mm; **d**,  $w$  [equals] 1.5 [thinsp] mm.  $N$  [equals] 12 experiments were carried out for each bridge width. Error bars indicate the standard deviation.

[High resolution image and legend \(41K\)](#)



We have identified the mechanism for this [lsquo]symmetry-restoring transition[rsquo] using experiments, analytical calculations and Monte Carlo simulations. **Figure 3b** shows that the proportion of experiments producing symmetrical flows on narrow bridges increases with the total number of ants crossing the bridge ( $[\chi]_2$  [equals] 4.6, d.f. [equals] 2,  $P$  [equals] 0.04). Moreover, **Fig. 3c** shows that both branches were equally used by the opposite flow directions. Therefore, in contrast to army ants<sup>6</sup> and pedestrians<sup>1</sup>, separation of the opposite flow directions was not found. This could be explained by a high level of disturbance, such as a large variation in the speeds of ants<sup>22</sup>.

The flow of ants over the bridge can be understood analytically. The concentration of the trail pheromone  $C_{ij}$  on branch  $i$  ( $i$  [equals] 1, 2) immediately behind each choice point  $j$  ( $j$  [equals] 1, 2) changes in time  $t$  according to:

$$dC_{ij}/dt = q\Phi_{ij}(t) + q\Phi_{ij'}(t - \tau) - \nu C_{ij}(t) \text{ with } j' = 3 - j \quad (1)$$

where  $[\Phi]_{i1}(t)$  represents the overall flow of foragers from the nest to the food source that choose branch  $i$  behind the choice point 1,  $[\Phi]_{i2}(t)$  is the opposite flow on branch  $i$  behind the other choice point  $j$  [prime] [equals] 3 -  $j$  [equals] 2,  $[\tau]$  is the average time required for an ant to get from one choice point to the other,  $q$  is the quantity of pheromone laid on the trail, and  $[\nu]$  is the decay rate of the pheromone. Moreover, if the density is low enough:

$$\Phi_{ij}(t) = \phi_j(t)F_{ij}(t) \quad (2)$$

where  $[\textit{phis}]_1$  is the outbound flow of foragers from the nest to the food source and  $[\textit{phis}]_2$  is the opposite, nestbound flow. The function  $F_{ij}$  describes the relative attractiveness of the trail on branch  $i$  at choice point  $j$ . For *L. niger* it is given by<sup>19</sup>:

$$F_{ij} = \frac{(k + C_{ij})^2}{(k + C_{1j})^2 + (k + C_{2j})^2} = 1 - F_{i'j} \text{ with } i' = 3 - i \quad (3)$$

where  $k$  denotes a concentration threshold beyond which the pheromone-based choice of a trail begins to be effective.

Equation (2) describes the flow dynamics without interactions between ants. However, when traffic was dense, we observed that ants that had just started to move on one branch were often pushed to the other branch, having collided frontally with another ant coming from the opposite direction. This behaviour will turn out to be essential in generating symmetrical traffic on narrow bridges. Whereas pushing was practically never observed on a 10-mm bridge, on narrow bridges the frequency of pushing events was high and proportional to the flow (**Fig. 3d**).

When pushing is taken into account, the overall flow of ants arriving at choice point  $j$  and choosing branch  $i$  can be expressed by the following formula:

$$\begin{aligned} \Phi_{ij}(t) = & \phi_j(t)F_{ij}(t)[1 - \gamma a \Phi_{ij'}(t - \tau)/w] \\ & + \phi_j(t)F_{i'j}(t)\gamma a \Phi_{i'j'}(t - \tau)/w \end{aligned} \quad (4)$$

The first term on the right-hand side of equation (4) represents the flow of ants engaged on branch  $i$  (that is,  $[\textit{phis}]_j(t)F_{ij}(t)$ ), diminished by the flow of ants pushed towards the other branch  $i$  [ $\textit{prime}$ ] by ants arriving from the opposite direction.  $a[\textit{Phi}]_{ij}[\textit{prime}](t - [\textit{tau}])/w$  is the proportion of ants decelerated by interactions. The factor  $a$  is proportional to the interaction time period and the lateral width of ants. Up to the symmetry-restoring transition it can be considered approximately constant.  $[\textit{gamma}]$  [ $\textit{ap}$ ] 0.57 denotes the probability of being pushed in the case of an encounter (**Fig. 3d**). The second term on the right-hand side of equation (4) represents the flow of ants that were engaged on branch  $i$  [ $\textit{prime}$ ] and were pushed towards branch  $i$ .

The stationary solutions of this model are defined by the conditions  $dC_{ij}/dt = 0$ ,  $F_{ij}(t - [\textit{tau}]) = F_{ij}(t)$ ,  $[\textit{Phi}]_{ij}(t - [\textit{tau}]) = [\textit{Phi}]_{ij}(t)$  and  $[\textit{phis}]_j(t - [\textit{tau}]) = [\textit{phis}]_j(t)$  (because the nestbound flow and the outbound flow should be equal). These imply:

$$C_{ij} = q(\Phi_{ij} + \Phi_{ij'})/\nu = C_{ij'} \quad F_{ij} = F_{ij'} = 1 - F_{i'j} = 1 - F_{i'j''}$$

and

$$C_{ij} = C_{ij'} = \frac{q\phi}{v} + D, \quad C_{i'j} = C_{i'j'} = \frac{q\phi}{v} - D \quad (5)$$

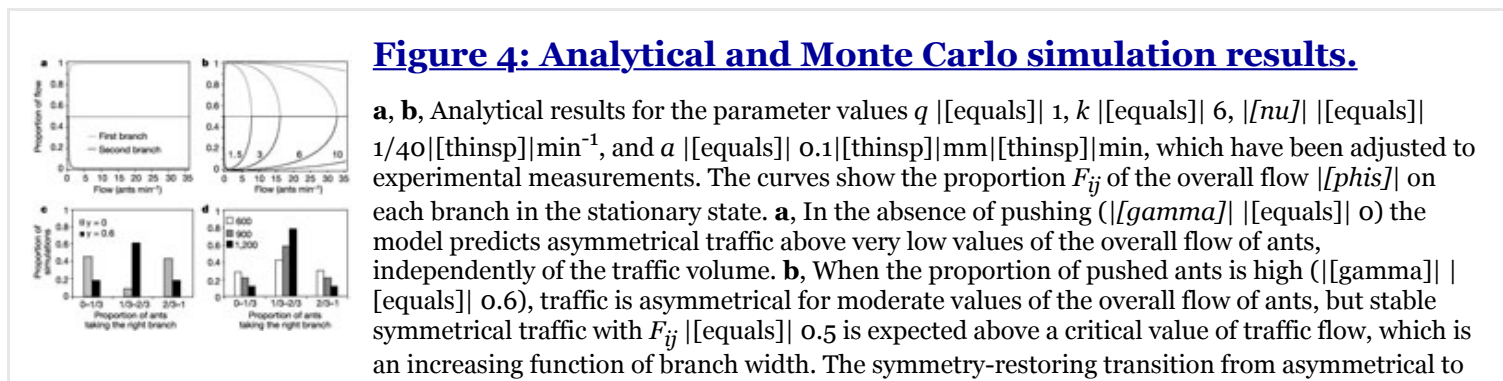
with

$$D = 0 \quad (6)$$

or

$$D^2 = \frac{q^2\phi^2}{v^2} - \frac{k^2 + \gamma a\phi(k + 2q\phi/v)^2/w}{1 + \gamma a\phi/w} \quad (7)$$

We can distinguish two cases. Case (1): when  $D^2 > 0$ , the stable stationary solution corresponds to asymmetrical traffic with  $C_{ij} = q\phi/v + \sqrt{D^2}$  and  $C_{i'j} = q\phi/v - \sqrt{D^2}$ . If  $\gamma = 0$ , this situation is given for  $q\phi/v > k$ . If  $q\phi/v < k$ , that is, if the pheromone concentration is too low, the ants choose both branches at random, corresponding to a symmetrical distribution (Fig. 4a). Case (2): when pushing is taken into account with  $\gamma > 0$ , the organization of traffic changes considerably: the asymmetrical solution can no longer be established as soon as  $D^2 < 0$  for large traffic volumes (Fig. 4b). In this case, symmetrical traffic is expected with  $C_{ij} = q\phi/v$  and  $\phi_{ij} = \phi/2$  for both branches  $i$  and choice points  $j$ . Therefore, high traffic volumes can be maintained and none of the branches is preferred in spite of the competitive effect due to the accumulation of pheromone on both branches. Moreover, the model implies that the outbound flow  $\phi_{i1}$  and the nestbound flow  $\phi_{i2}$  are equal, indicating that one-way flows are not required to maintain a high traffic volume<sup>23</sup>. These analytical results have been confirmed by Monte Carlo simulations (see Fig. 4c, d). Our simulations have also demonstrated that if pushed ants, instead of moving to the other branch, made a U-turn and returned in the direction they had been coming from, the overall flow of ants crossing the bridge was affected by the branch width and no shift to symmetrical traffic was observed.



symmetrical traffic flow corresponds to an inverse pitchfork bifurcation. **c, d**, Results of Monte Carlo simulations. At time  $t = 0$ , the pheromone concentration and the number of ants on each branch are set to zero. Ants arrive at choice point  $j$  at a rate  $|\phi_j(t)| = |\phi_j|$ . The probability of choosing the right or left branch at a choice point is governed by the choice function  $F_{ij}$  (see equation (3)). However, as soon as an ant has engaged on a branch, it may be pushed to the other branch with probability  $|\gamma|$  by an ant moving in the opposite direction coming from the second choice point. The pushed ant then continues its course on the alternative branch and lays a trail. For each value of  $|\gamma|$ , the simulations are averaged over 1,000 runs. The graphs show the relative frequency of simulations in which a certain proportion of traffic was supported by the right branch. **c**, Assuming a pushing probability equal to zero ( $|\gamma| = 0$ ), most simulations ended with asymmetrical traffic. However, when we used the experimental value  $|\gamma| = 0.6$ , most simulations for narrow branches resulted in symmetrical traffic. **d**, The proportion of simulations with  $|\gamma| = 0.6$  in which asymmetrical traffic emerged is a function of the total number of ants crossing the bridge, just as in our experiments (compare Fig. 3b).

### [High resolution image and legend \(56K\)](#)

The traffic organization in ants can be called optimal. The overall flow on branch  $i$  behind choice point  $j$  is given by  $|\Phi_{ij}| = w|\rho_{ij}|V_{ij}$ , where  $|\rho_{ij}|$  denotes the density of ants. Their average speed is theoretically estimated by  $V_{ij} = V_m(1 - a|\Phi_{ij}|/w)$ , where  $V_m$  denotes the average maximum speed and  $a|\Phi_{ij}|/w$  is again the proportion of decelerated ants. For the symmetry-restoring transition with  $D^2 = 0$ , equation (7) requires  $a|\gamma||\phi_j|/w < 1/3$ , which implies  $V_{ij} > V_m[1 - 1/(3|\gamma|)] = 0.42V_m$ . However, according to the empirical speed-density relation by Burd *et al.*<sup>23</sup>, the maximum flow (the capacity) is only reached at the smaller speed  $V_{ij} = V_m[1 - 1/(n + 1)] = 0.39V_m$ . Although the empirical value  $n = 0.64$  was determined for another ant species, the values for *L. niger* should be comparable. This shows that the symmetry-restoring transition occurs before the maximum flow is reached. The strict inequality also implies capacity reserves and a limitation of the density-related speed reduction. A marginal reduction in speed, however, would not favour symmetrical traffic because of the benefits of using a single trail. First, a more concentrated trail provides a better orientation guidance and a stronger arousal stimulus<sup>24</sup>. Second, a higher density of ants enhances information exchange and supports a better group defence<sup>25</sup>.

We have demonstrated the surprising functionality of collisions among ants to keep up the desired flow level by generation of symmetrical traffic. Pushing behaviour may be considered an optimal behaviour to maintain a high rate of food return to the nest. It would not be required in most models of ideal free distribution (IDF)<sup>26</sup>, as they neglect effects of inter-attraction. The balancing between cohesive and dispersive forces avoids a dysfunctional degree of aggregation and supports an optimal accessibility of space at minimal costs allowing an efficient construction, maintenance and use of infrastructures. This mechanism appears to be generic in nature, in particular in group-living organisms. For example, inhibitory interactions at overcrowded building sites in termites allow a smooth growth of the nest structure<sup>27</sup>. In the development of urban agglomerations such interactions help to maintain the coexistence of distinct cities<sup>28</sup>, and in vehicle traffic they determine the choice of longer, less congested routes. The mechanism also suggests algorithms for

the routing of data traffic in networks.

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## Competing interests statement

The authors declare no competing financial interests.



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